

提出期限：平成22年 6月 14日

演習第七

1. Consider the following language $L = \{0^n 1^m \mid n, m \in \mathbb{N} \text{ and } m \leq n^2\}$. Prove or disprove L to be context-free.

2. Consider the following grammar $\mathcal{G} = [\{a, b\}, \{\sigma, \alpha, \beta, \gamma\}, \sigma, P]$, where

$$P = \{\sigma \rightarrow a\alpha a, \alpha \rightarrow \sigma b, \alpha \rightarrow b\beta\beta, \beta \rightarrow abb, \gamma \rightarrow a\beta\}$$

Construct a grammar \mathcal{G}' such that \mathcal{G}' is reduced and equivalent to \mathcal{G} .

3. Prove or disprove $L = \{a^{n^2} \mid n \in \mathbb{N}\}$ to be context-free.