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演習第十三

Solve at least three of the following four problems.

1. Prove or disprove the following:

There exists a function $f \in \mathcal{P}$ such that there is no function $g \in \mathcal{R}$ with $f \subseteq g$.

2. Let $S = \{i \mid i \in \mathbb{N} \text{ and } U(i, x) \text{ stops for all } x \in \mathbb{N}\}$.

Prove or disprove the following: S is decidable.

3. Let $A, B \subseteq \mathbb{N}$. Prove or disprove the following assertions to be true.

- (a) If A and B are decidable then $A \cup B$ is decidable.
- (b) If A and B are decidable then $A \setminus B$ is decidable.
- (c) If $\mathbb{N} \setminus A$ is finite, then A is decidable.
- (d) There exists a set A such that A and $\mathbb{N} \setminus A$ are both undecidable.

4. Show the relation \leq_{red} to be transitive.